





Bridge Circuits











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- This material is based upon work supported by the National Science Foundation's Advanced Technological Education Program under Grant No. 1801177.
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Bridge Circuits

- A bridge circuit is a specific type of circuit that has a <u>bridging</u> section usually between two parallel sections.
- Here are several common types of bridge circuits.





- The Wheatstone Bridge is probably the most common type of bridge circuit.
- It is used in numerous applications:
 - Digital Scales (i.e. digital bathroom scales, postage scales, etc.)
 - Ohmmeters
 - Load cells (used in tensile testing machines)
- Let's look how the circuit works by first simplifying and labeling it.







- It can be seen in this new arrangement the bridge circuit is just two voltage divider circuits in parallel.
- The supply voltage V_s is called the excitation voltage.
- Let's label the various nodes now.
- The current through *ABC* is

$$I_{ABC} = \frac{V_S}{R_1 + R_2}$$

• Likewise, the current through ADC is

$$I_{ADC} = \frac{V_s}{R_3 + R_4}$$





• The voltage at nodes *B* and *D* may then be found by

$$V_B = I_{ABC}R_2 = \frac{V_sR_2}{R_1 + R_2}$$
 and $V_D = I_{ADC}R_4 = \frac{V_sR_4}{R_3 + R_4}$

• The voltage between the two nodes is then

$$V_o = V_D - V_B = \frac{V_S R_4}{R_3 + R_4} - \frac{V_S R_2}{R_1 + R_2}$$
$$= V_S \frac{R_1 R_4 - R_2 R_3}{(R_1 + R_2)(R_3 + R_4)}$$

• V_o is known as the output voltage.



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- Let's look at some special cases of the circuit.
- What is V_o when $R_1 = R_2 = R_3 = R_4$?
 - $V_o = 0V$
 - When the <u>output voltage is zero</u>, the circuit is said to be <u>balanced</u>.
- What is V_o when $R_1 = R_2 = R_3 \neq R_4$?
 - $V_o \neq 0V$
 - When the <u>output voltage is not zero</u>, the circuit is said to be <u>unbalanced</u>.
 - This imbalanced can be related to the amount of change that is experienced in *R*₄.

$$V_o = V_s \frac{R_1 R_4 - R_2 R_3}{(R_1 + R_2)(R_3 + R_4)}$$





• Let's denote the starting value of R_4 as R_0 . $R_4 = R_0 + \Delta R_4$

where ΔR_4 is the amount of change in R_4 .

• V_o is then

 $V_o = V_s \frac{R_1(R_0 + \Delta R_4) - R_2 R_3}{(R_1 + R_2)[R_3 + (R_0 + \Delta R_4)]}$

• Solving for ΔR_4 shows

 $\Delta R_4 = \frac{V_s(R_1R_0 - R_2R_3) - V_o(R_1 + R_2)(R_3 + R_0)}{V_0(R_1 + R_2) - V_sR_1}$

$$V_o = V_s \frac{R_1 R_4 - R_2 R_3}{(R_1 + R_2)(R_3 + R_4)}$$





- Why is this important/useful?
 - A lot of sensors change their resistance based on the conditions they are experiencing (for example, the thermistor).
 - The Wheatstone Bridge can be used to measure these changes in resistance.
- Why not just use a simple voltage divider circuit?
 - A simple voltage divider circuit is sensitive to slight unintended changes in resistance in either the top or bottom resistors.
 - The Wheatstone Bridge overcomes this issue by being somewhat self balancing.
 - That is the circuit auto adjusts to unintended changes in resistances.

IMPIF†

$$V_o = V_s \frac{R_1 R_4 - R_2 R_3}{(R_1 + R_2)(R_3 + R_4)}$$



Let's Build The Circuit

• Build a Wheatstone bridge circuit using three $10k\Omega$ resistors and your thermistor as shown below.





• With multimeter set to reading DC voltage, what does it read?



• Is the bridge circuit balanced?



Let's Build The Circuit

- More than likely, your circuit is not balanced. Why?
- What can we do to make it balanced?
- Using a potentiometer, we can balance the circuit ourselves without the need to obtain resistors that are exactly the same resistance values.
- Build the circuit shown below using the potentiometer in place of R_3 .







Let's Build The Circuit

- Now that the potentiometer is implemented, adjust the potentiometer until the multimeter reads zero.
- Once the multimeter reads zero volts, the bridge is balanced.
- What happens now when you touch the thermistor?
- What happens when you make the thermistor colder?



