## Math for Laser and Optics Technicians

### **Angle Measurements**

Photonics technicians need to perform calculations using angles measured in both degrees and radians, converting between the two, if necessary, by using the equivalency between  $2\pi$  radians and 360 degrees. They also need to calculate partial solid angles (in three dimensions), such as the solid angle subtended by a beam of light emanating and spreading out from a point source of light.

#### **EXAMPLE**

Laser light exiting an Nd:YAG laser passes through an exit aperture (opening) at the output laser mirror of diameter 1 millimeter. The wavelength of light for an Nd:YAG laser is 1.06  $\mu$ m. You have learned that the beam spread of light of wavelength,  $\lambda$ , through a circular opening of diameter, *D*, is given by the equation.

$$\Theta = 1.27 \frac{\lambda}{D}$$

Where  $\boldsymbol{\Theta}$  is the beam angle spread (called divergence) and is given in radian measure.

#### Question

For this laser, determine the beam spread angle in both radians and degrees.



Geometry



# **Solution to Geometry Question**

Beam spread angle  $\Theta$  in radians is given  $\Theta = 1.27 \frac{\lambda}{D}$ 

Therefore, 
$$\Theta_{rad} = \frac{(1.27)(1.06 \times 10^{-6} \text{ yr})}{1 \times 10^{-3} \text{ yr}} = 1.35 \times 10^{-3} \text{ radians}$$

= 1.35 milliradians

Now, converting to degrees:

$$\frac{1.35 \times 10^{-3} \text{ rad}}{\pi \text{ rad}} = 0.077^{\circ}$$

The beam spread of laser beams (here less than one tenth of a degree!) is much smaller than that of flashlights, searchlights, and so on.

