## Math for Laser and Optics Technicians

## Angle Measurements

Photonics technicians need to perform calculations using angles measured in both degrees and radians, converting between the two, if necessary, by using the equivalency between $2 \pi$ radians and 360 degrees. They also need to calculate partial solid angles (in three dimensions), such as the solid angle subtended by a beam of light emanating and spreading out from a point source of light.

## EXAMPLE

Laser light exiting an Nd:YAG laser passes through an exit aperture (opening) at the output laser mirror of diameter 1 millimeter. The wavelength of light for an Nd:YAG laser is $1.06 \mu \mathrm{~m}$. You have learned that the beam spread of light of wavelength, $\lambda$, through a circular opening of diameter, $D$, is given by the equation.

$$
\theta=1.27 \frac{\lambda}{D}
$$



Where $\Theta$ is the beam angle spread (called divergence) and is given in radian measure.

## Question

For this laser, determine the beam spread angle in both radians and degrees.

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## Solution to Geometry Question

Beam spread angle $\theta$ in radians is given $\quad \theta=1.27 \frac{\lambda}{D}$

$$
\text { Therefore, } \begin{aligned}
\Theta_{\mathrm{rad}}=\frac{(1.27)\left(1.06 \times 10^{-6} \mathrm{mx}\right)}{1 \times 10^{-3} \mathrm{~m}} & =1.35 \times 10^{-3} \text { radians } \\
& =1.35 \text { milliradians }
\end{aligned}
$$

Now, converting to degrees:

$$
\begin{array}{l|l}
1.35 \times 10^{-3} \mathrm{rad} & 180^{\circ} \\
\hline & \pi \text { rad }
\end{array}=0.077^{\circ}
$$

The beam spread of laser beams (here less than one tenth of a degree!) is much smaller than that of flashlights, searchlights, and so on.
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