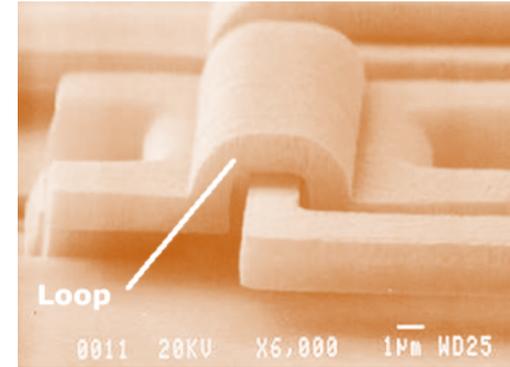




SCME

Support Center for
Microsystems Education



Introduction to Statistical Process Control (SPC) For Technicians

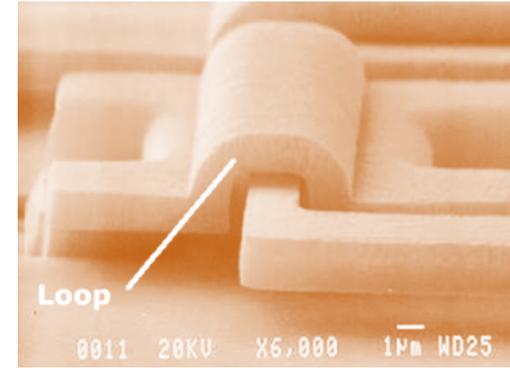
Support Center for
Microsystems Education

-SCME-
2017



SCME

Support Center for
Microsystems Education



SCME is a National Science Foundation Advanced Technological Education (ATE) Support Center at the University of New Mexico.

We offer professional development and educational materials to excite and engage community college, university, and high school students and faculty in the field of Microsystems (Micro Electro Mechanical Systems, MEMS) technology.

Support for this work was provided by the National Science Foundation's Advanced Technological Education (ATE) Program through Grants #DUE 1205138 & 1700678 .

SEM of Loop and Hinge System Courtesy of Sandia National Laboratories



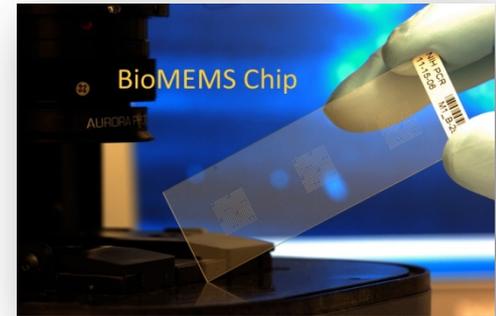
Objectives

- Process variation and the need to identify special cause variation
- Statistical Process Control (SPC)
- Statistical tools necessary to employ SPC

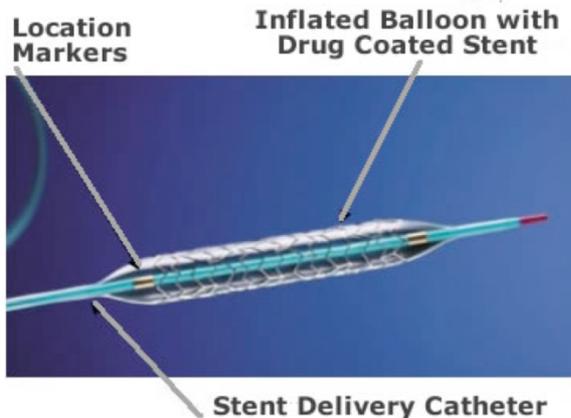
Why do we need (SPC) Statistical Process Control?



Quality Product

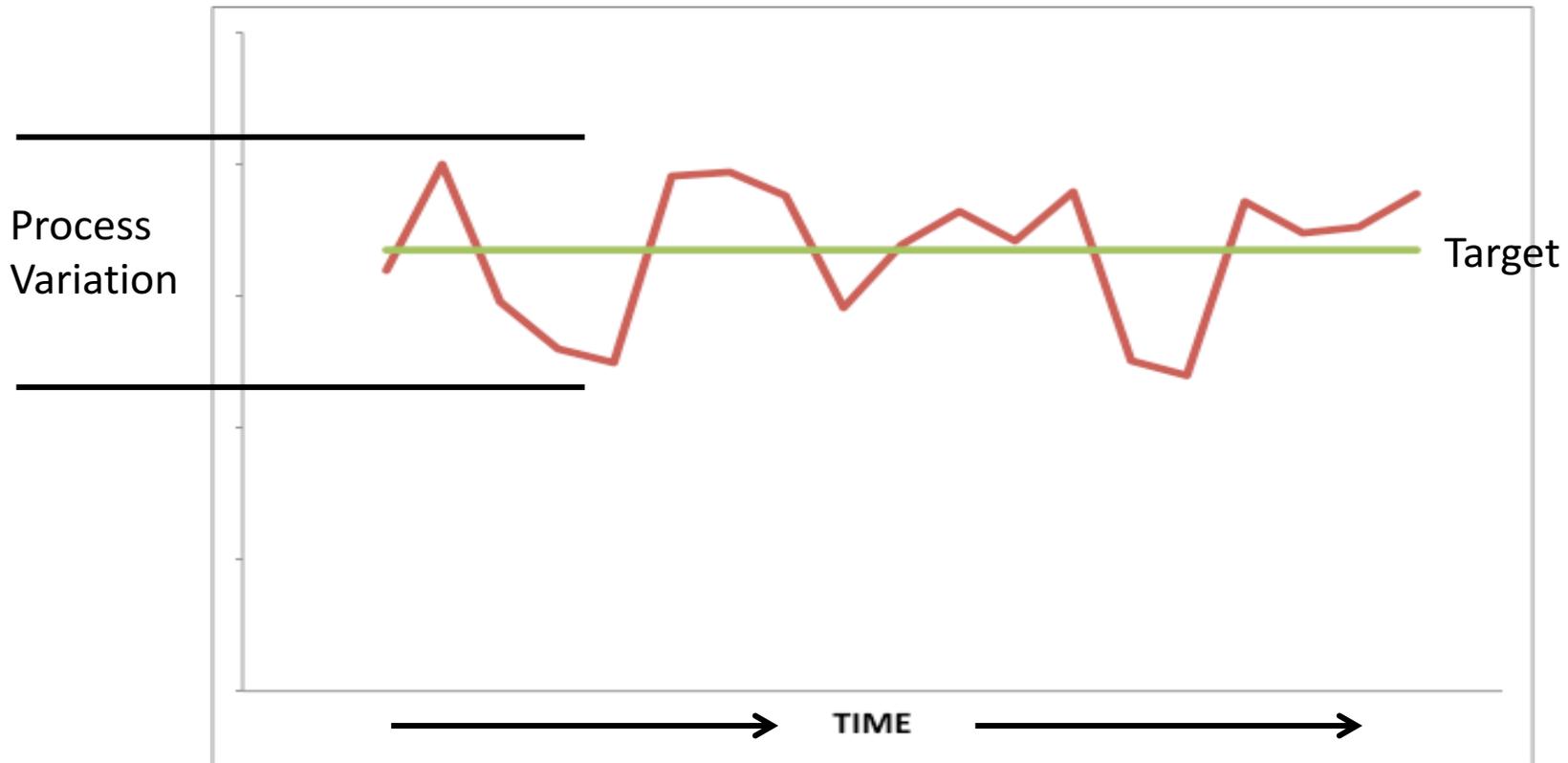


*Biochip slide for testing protein arrays
[Image courtesy of Argonne National Laboratories]*



Statistical Process Control (SPC)

SPC is about “control”.

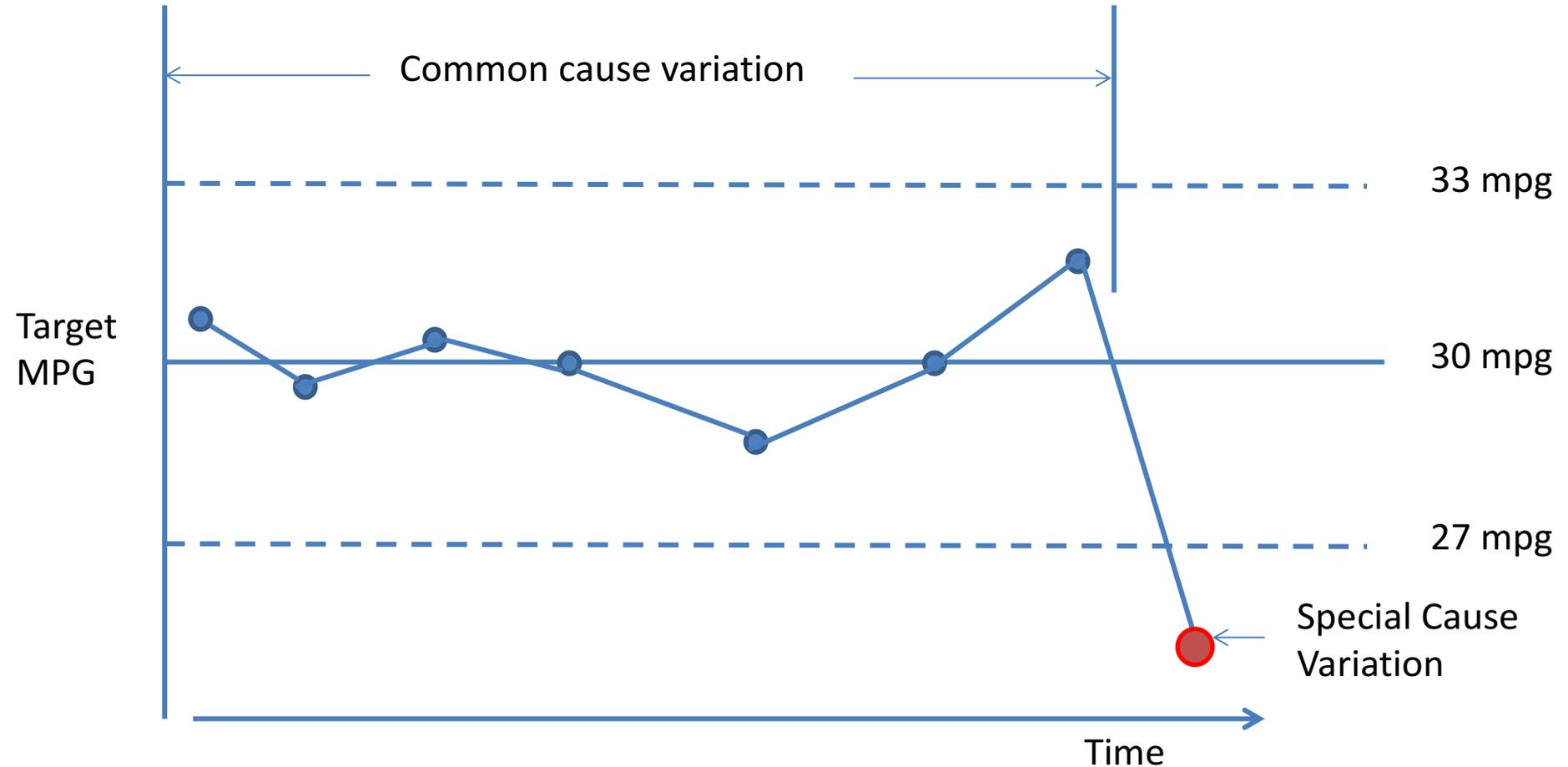


Inherent or Common Cause Variation



Special Cause Variation

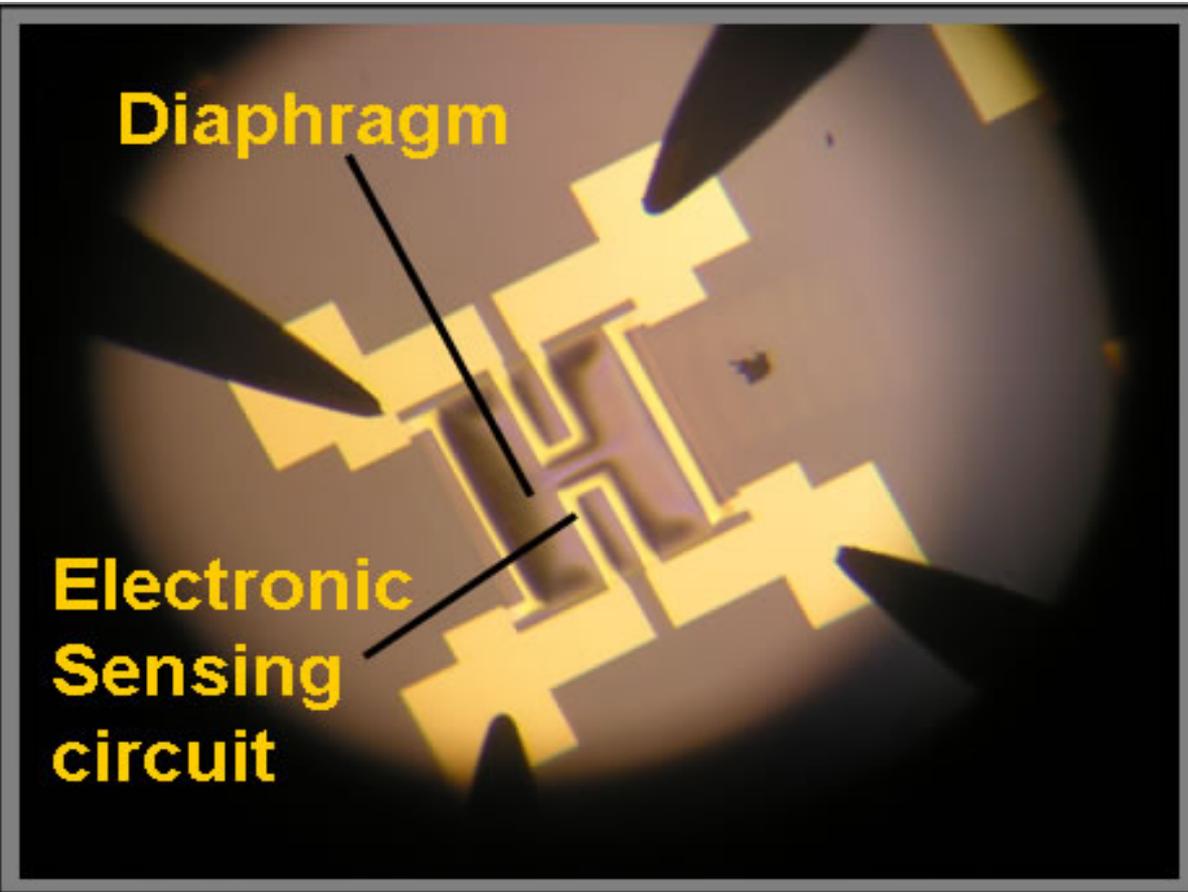
Tracking Your Gas Mileage



Special Cause Variability

Process Steps:

1. Silicon Nitride Deposition
2. Lithography for chamber
3. Lithography for sensing circuit
4. Metal deposition for circuit
5. Metal Removal
6. Etch reference chamber



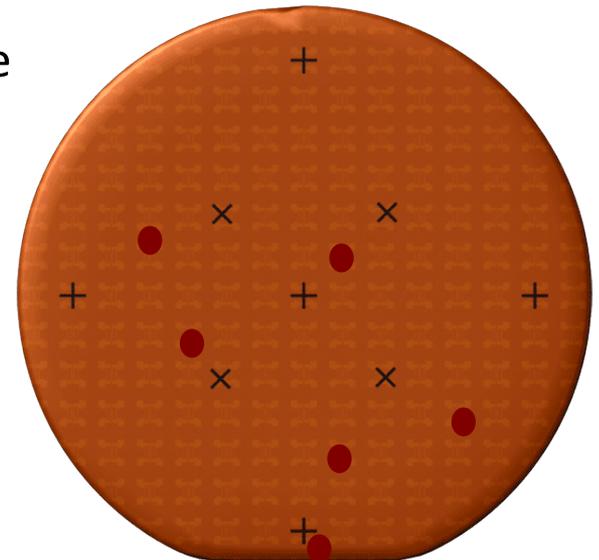
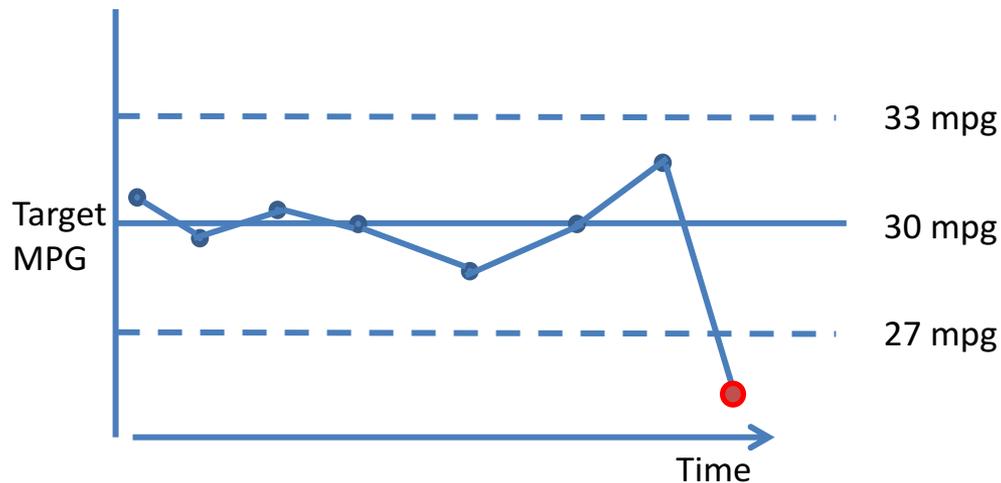
Diaphragm

The image shows a micrograph of a microsystem device. It features a central square chamber with a complex internal structure. The chamber is surrounded by a network of metal lines and pads. The device is mounted on a substrate, and the overall appearance is that of a precision-machined microcomponent. The labels 'Diaphragm' and 'Electronic Sensing circuit' are overlaid on the image in yellow text, with black lines pointing to the corresponding parts of the device.

**Electronic
Sensing
circuit**

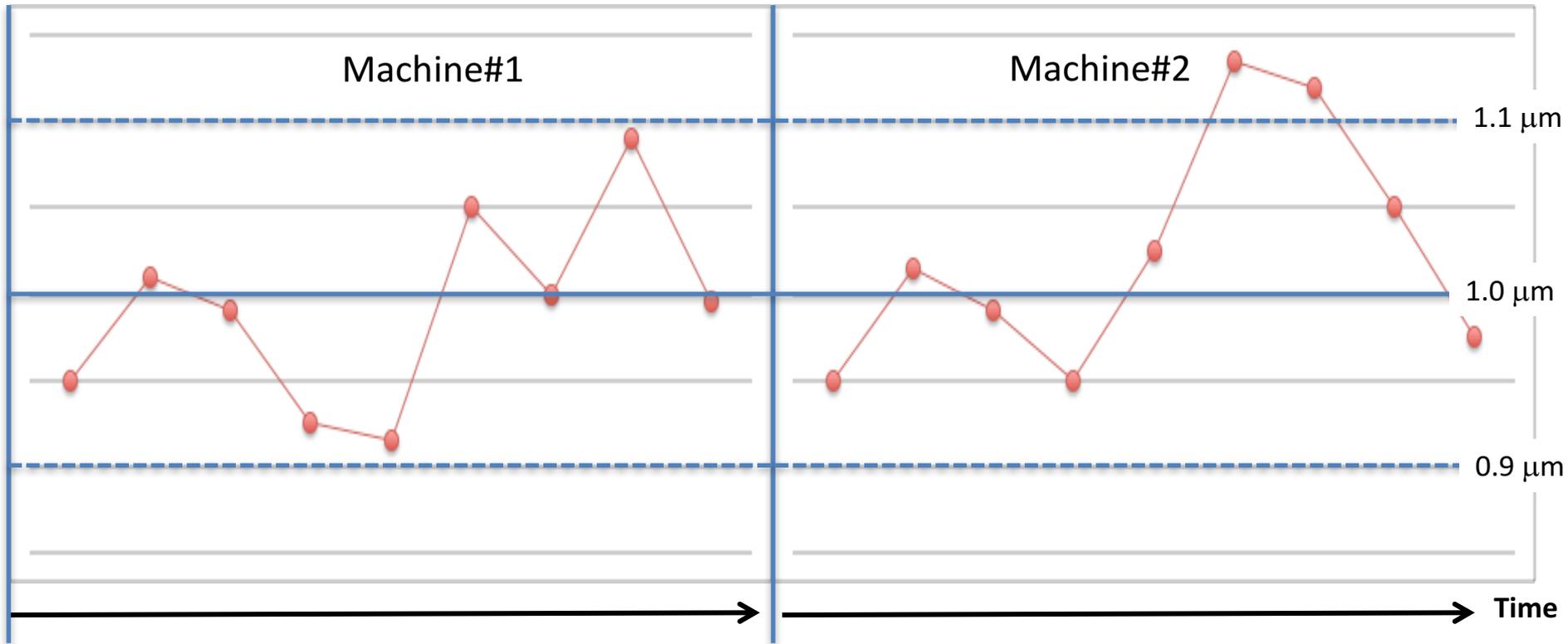
Types of data

- Variable Data
 - Data Based upon measurements
 - Length, time, weight, temperature, pressure, film thickness
- Attribute Data
 - Data based upon counts (discrete)
 - Either there or not
 - Number of defects, acceptable or unacceptable



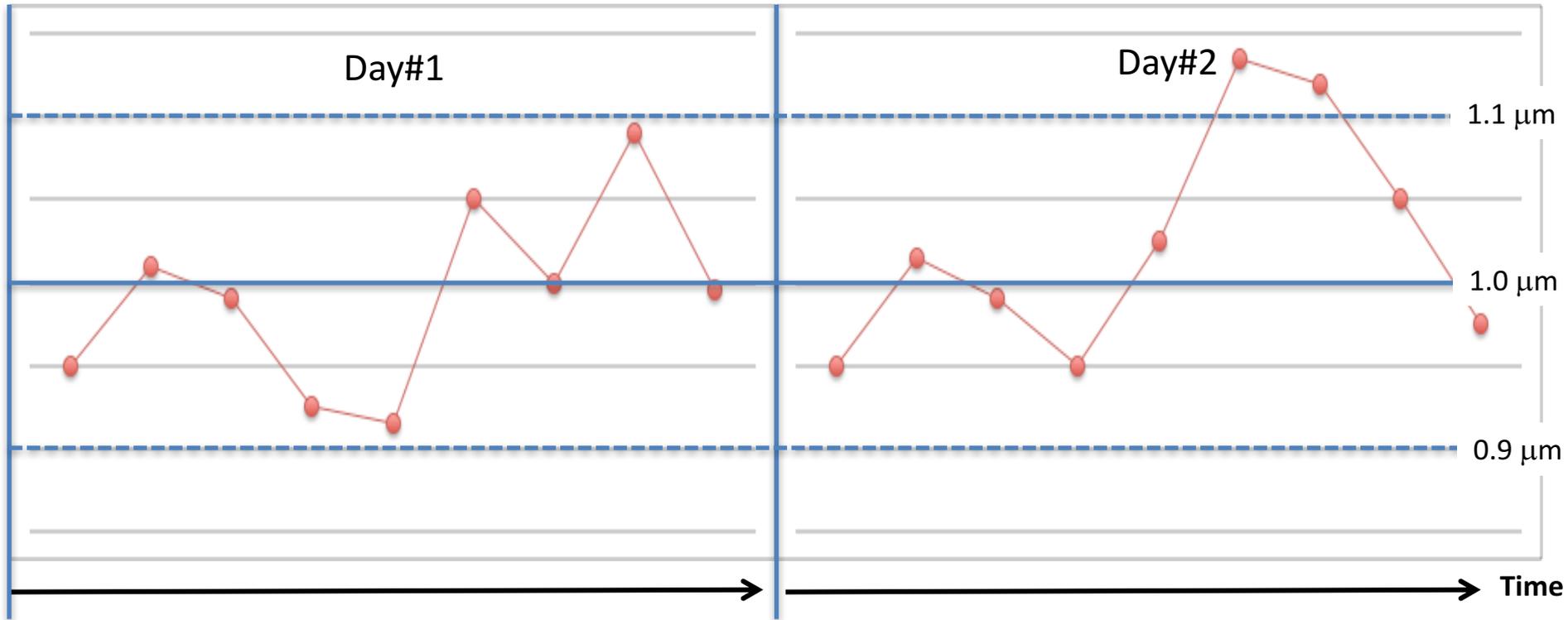
Variability

Photoresist Thickness



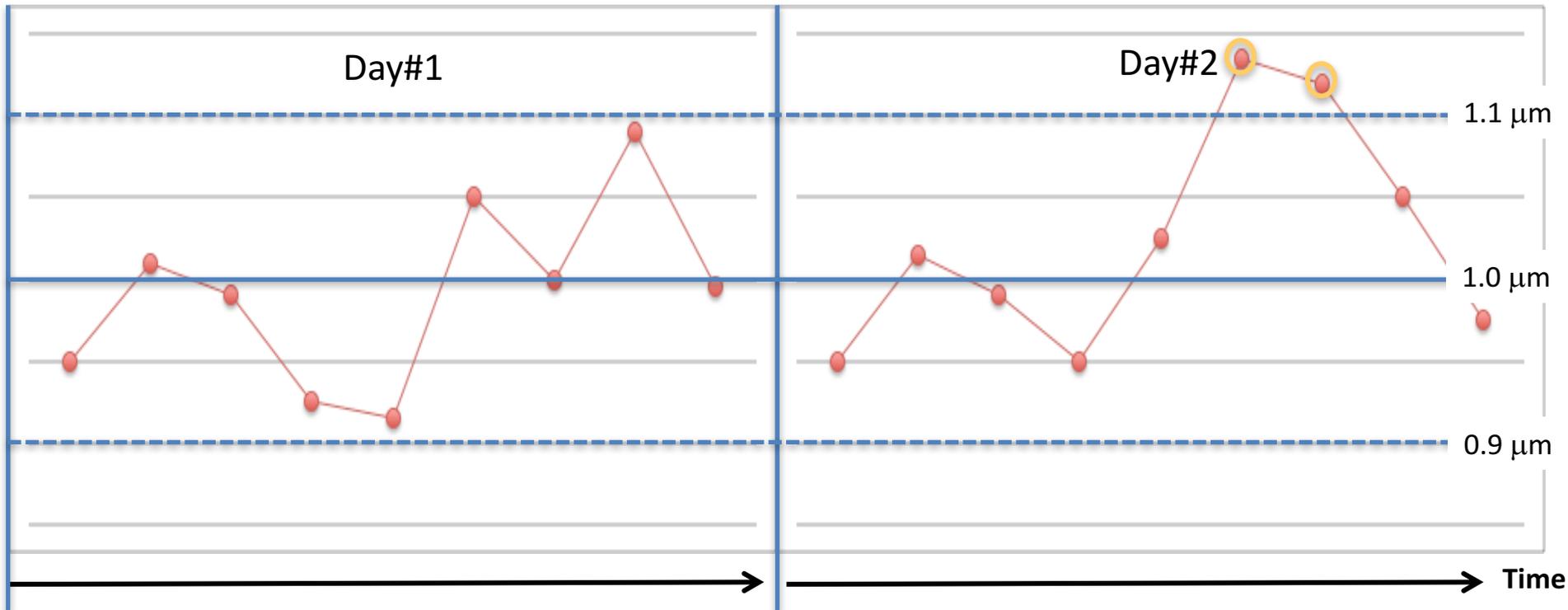
Variability

Photoresist Thickness



Variability

Photoresist Thickness

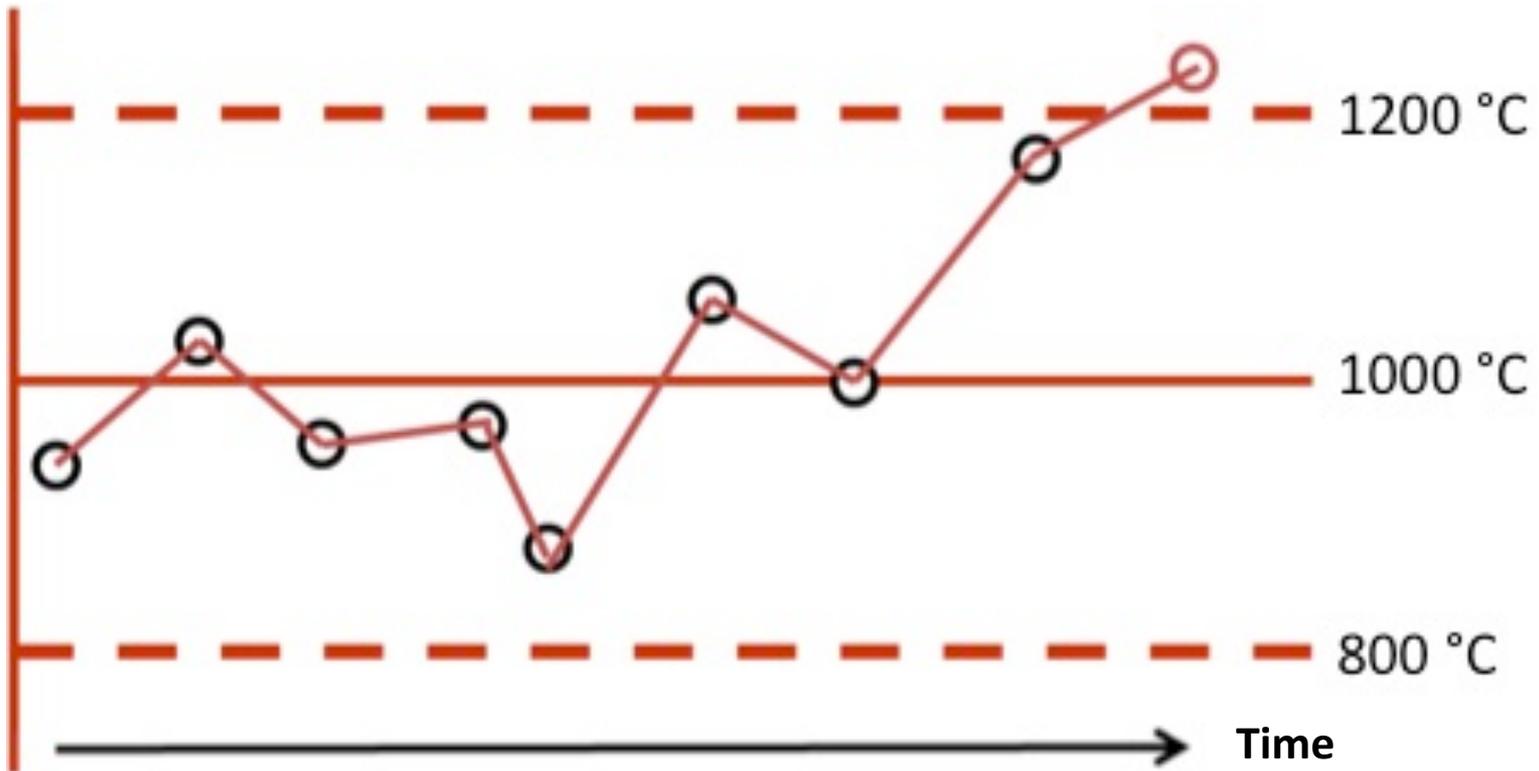


Common Cause Variation
Controlled Variation

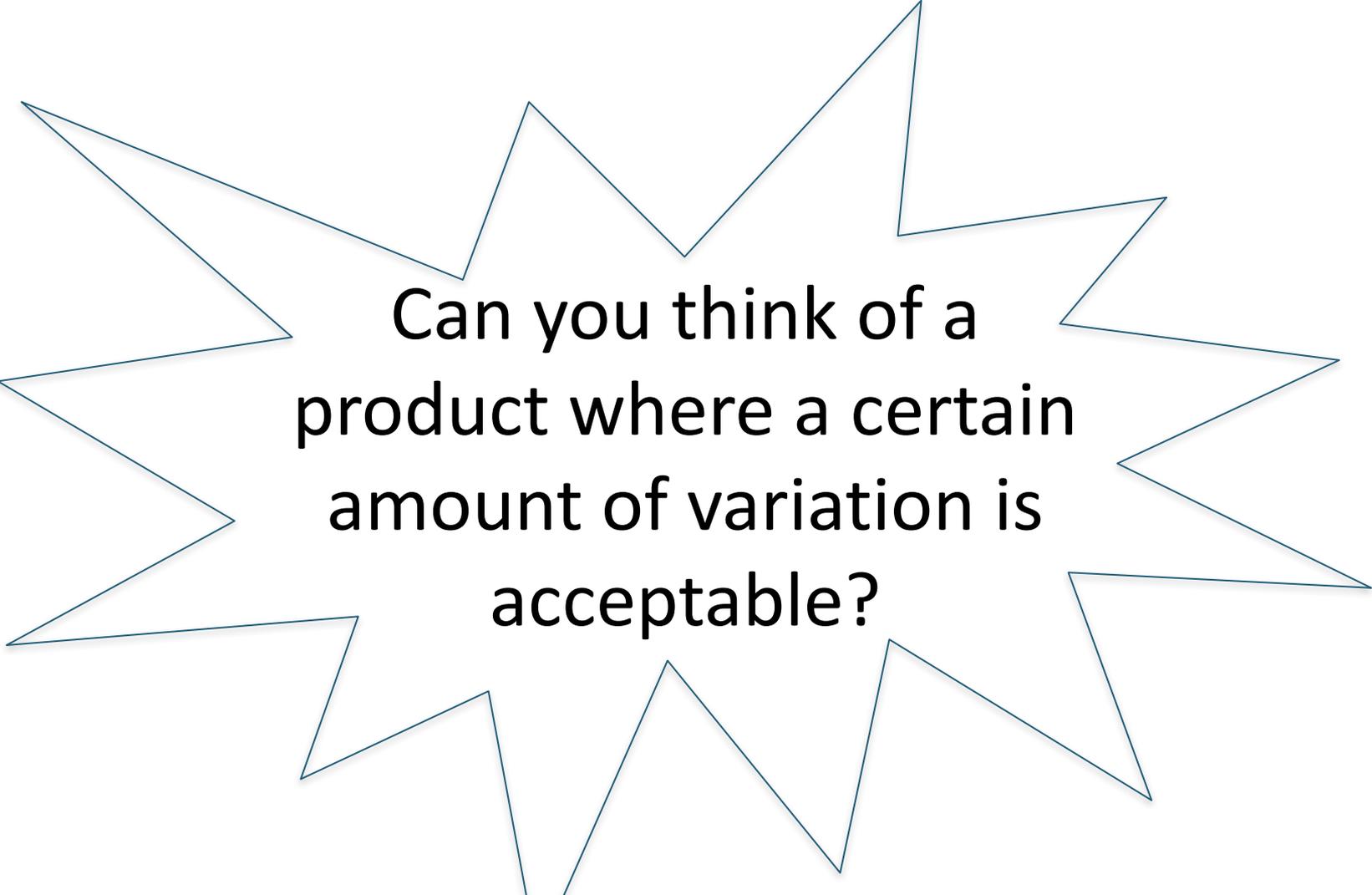
Special Cause Variation
Uncontrolled Variation

Another Example

Process Temperature



Desired Variation



**Can you think of a
product where a certain
amount of variation is
acceptable?**

Desired Variation

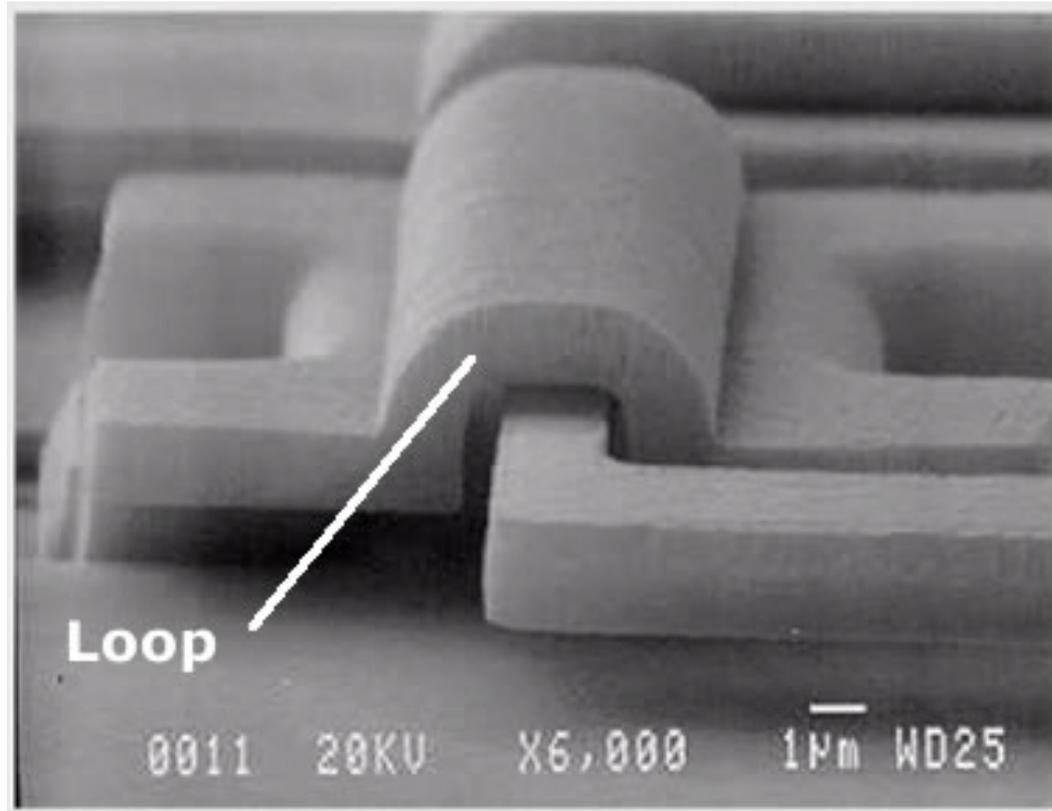


Can you think of a
product where a certain
amount of variation is
acceptable?

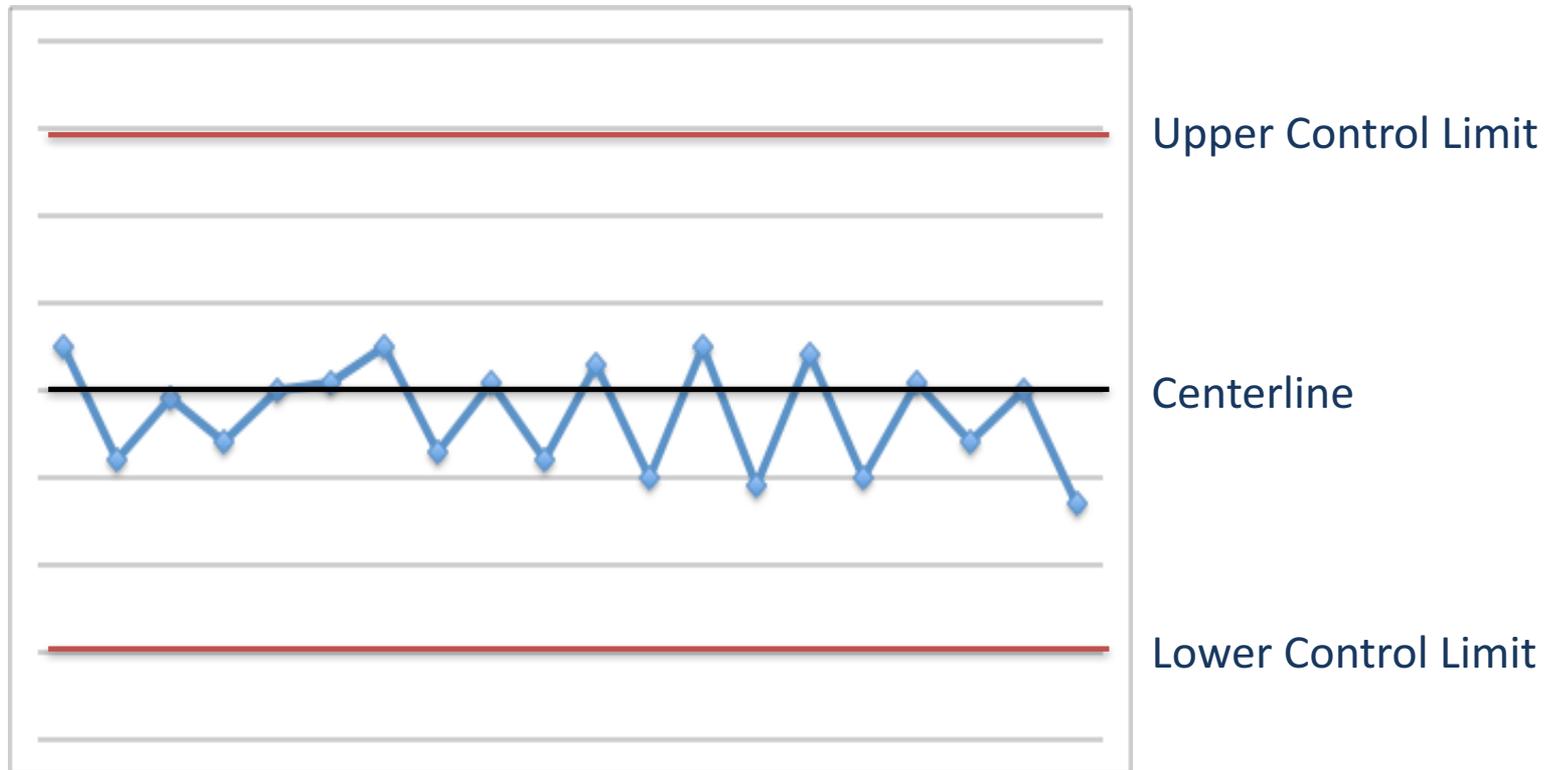


Variation in Microsystems

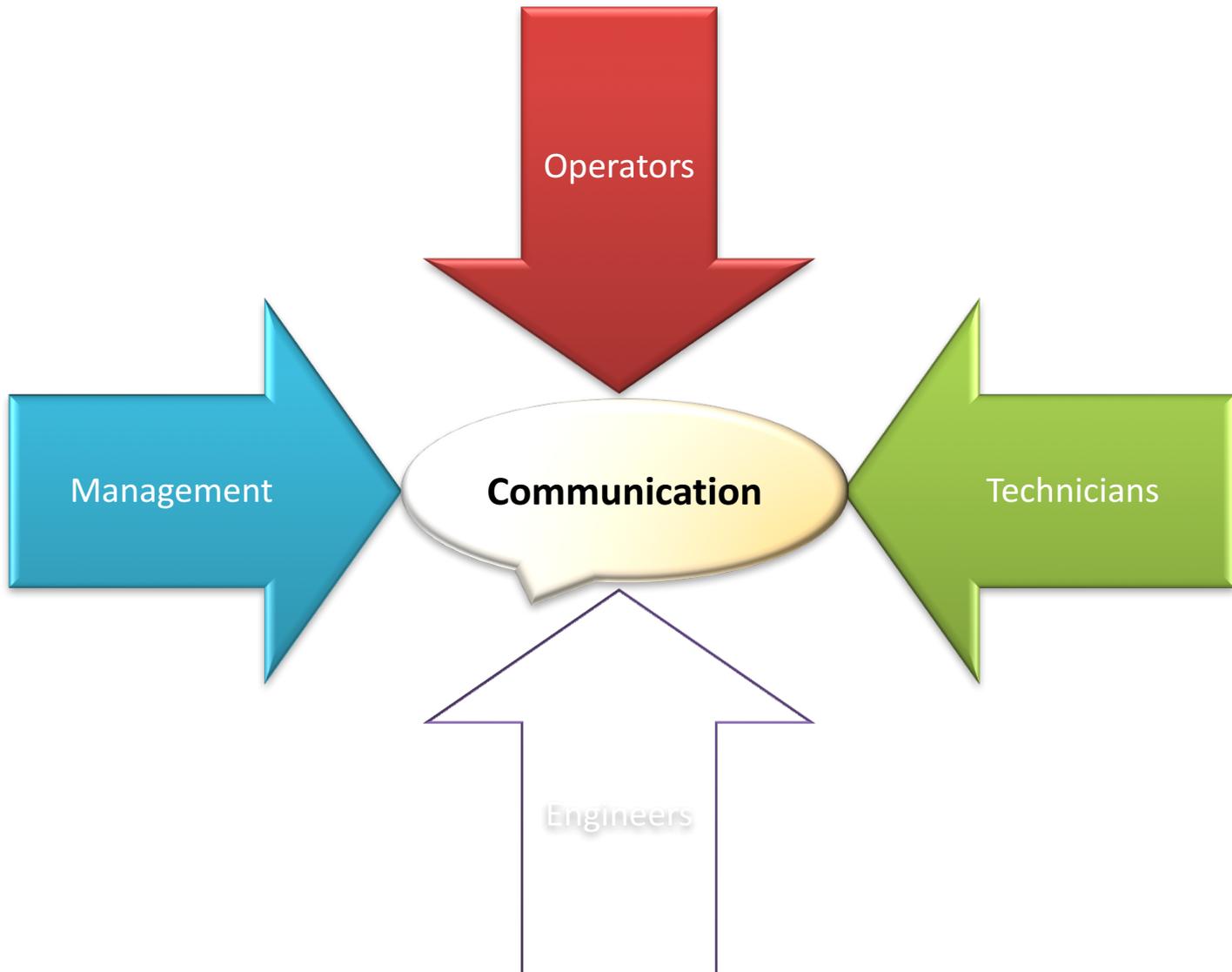
Hinge System



Statistical Process Control and Variation

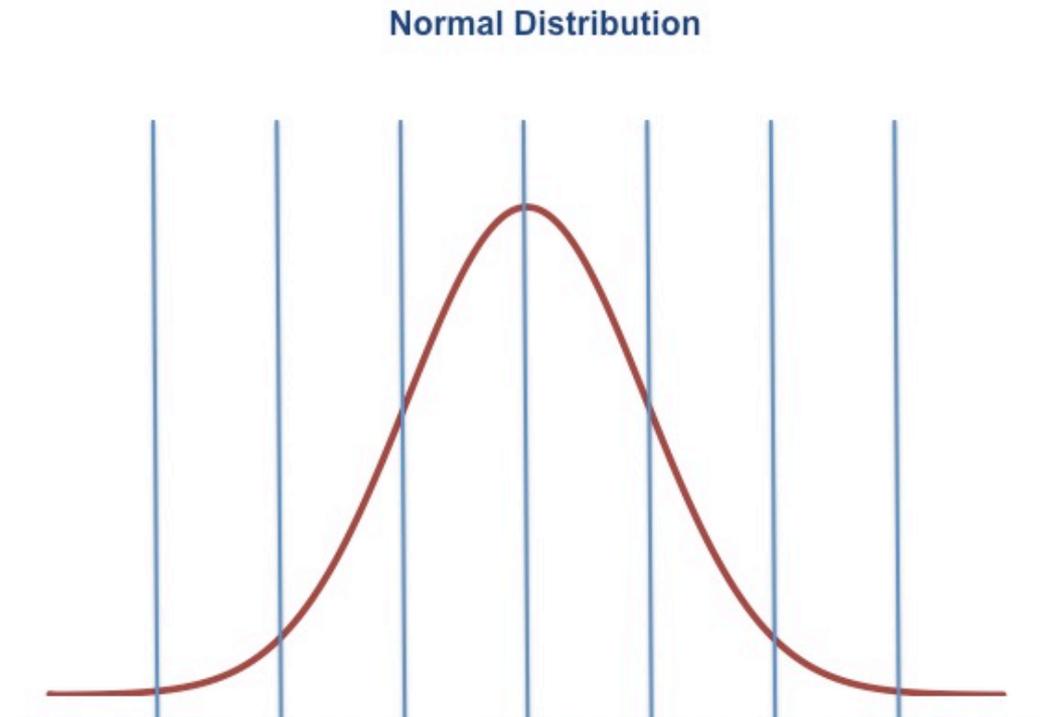


Communication is KEY!



Statistics for Statistical Process Control

- Statistics for Central Tendency
 - Sample Median
 - Sample Mean
- Statistics for Variability
 - Sample Range
 - Sample Variance
 - Sample Standard Deviation



Sample Median – Central Tendency

Sample Median

- Represents the data value that is “physically” in the middle of the sample set when arranged in numerical order.

Example:

- Given the data set: 2,4,1,5,3
- Order the data: 1,2,3,4,5
- **Question: What is the Median?**

Sample Median – Central Tendency

Sample Median

- Represents the data value that is “physically” in the middle of the sample set when arranged in numerical order.

Example:

- Given the data set: 2, 4, 1, 5, 3
- Order the data: 1, 2, **3**, 4, 5

Example:

- Given the data set: 2, 4, 1, 5, 1, 3
- Order the data: 1, 1, 2, 3, 4, 5
- Median is the average of the 2 middle #'s: 2 and 3
- Median = **2.5**

Sample Mean – Central Tendency

Mean

- Universal or Arithmetic Mean = μ
- Sample Mean = \bar{X}
- Mean of a collection of sample Means = $\bar{\bar{X}}$

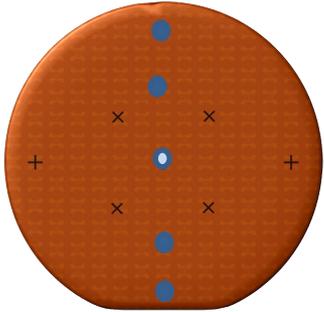
Calculation of Mean

$$\mu = \frac{\sum x_n}{n}$$

5 Resist Thickness Values: 2.87, 2.99, 3.01, 3.15, 2.98 Microns

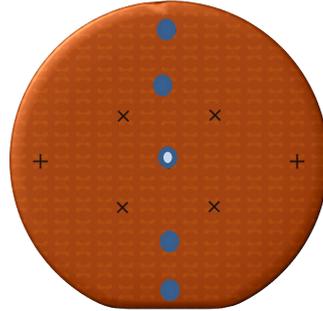
$$\mu = \bar{X} = \frac{2.87 + 2.99 + 3.01 + 3.15 + 2.98}{5} = 3.00 \text{ microns} \quad \text{Sample Mean}$$

What is $\bar{\bar{X}}$?



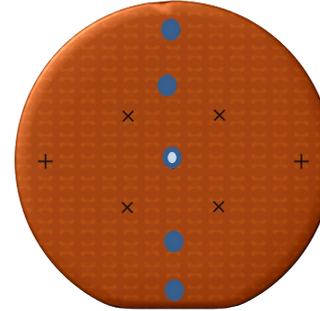
Wafer #1

3.23
3.09
4.82
4.16
2.11



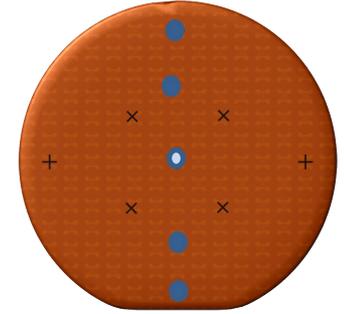
Wafer #2

3.43
4.29
1.95
4.55
2.37



Wafer #3

3.74
2.01
1.58
4.89
1.38



Wafer #4

2.52
2.49
1.68
4.18
1.61

$\bar{\bar{X}}$

Wafer #1 Sample Mean

$\bar{X} = 3.48$
microns

Wafer #2 Sample Mean

$\bar{X} = 3.32$
microns

Wafer #3 Sample Mean

$\bar{X} = 2.72$
microns

Wafer #4 Sample Mean

$\bar{X} = 2.49$
microns

$$\bar{\bar{X}} = \frac{3.48 + 3.32 + 2.72 + 2.49}{4} = 3.00 \text{ microns}$$

Sample Range

Statistics for Variability

Statistics for Variability

- Sample Range
- Sample Variance
- Sample Standard Deviation

- *Sample Range*

- The difference between the maximum value minus the minimum value.

2.87, 2.99, 3.01, 3.15, 2.98

Question – What is the Sample Range?

Sample Range

Statistics for Variability

Statistics for Variability

- Sample Range
- Sample Variance
- Sample Standard Deviation

- *Sample Range*

- The difference between the maximum value minus the minimum value.

2.87, 2.99, 3.01, 3.15, 2.98

$$3.15 - 2.87 = 0.28 \text{ Sample Range}$$

Sample Variance

Statistics for Variability

- *Sample Variance*
 - How far a set of numbers are spread out.

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \mu)^2}{n - 1}$$

- 5 Resist Thickness Values: 2.87, 2.99, 3.01, 3.15, 2.98 microns
- Mean = 3.00 microns
- $\sigma^2 = 0.01$ Square Microns

Sample Standard Deviation

Statistics for Variability

- *Sample Standard Deviation*

- Measurement of how the data are distributed around the sample mean and within a range of values.

$$\sigma = \sqrt{\sigma^2} = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu)^2}{n - 1}}$$

- $\sigma^2 = 0.01 \text{ micron}^2$
- $\sigma = 0.1 \text{ micron}$

Summary

- SPC is a statistical scientific method that provides valuable information about a process
- This type of variation (common and special cause) should be understood and controlled.
- Statistical Concepts used in SPC
 - Sample median
 - Sample mean – μ , \bar{X} , $\bar{\bar{X}}$
 - Sample range - R
 - Sample variance – σ^2
 - Sample standard deviation – σ